

## SESIONES ESPECIALES

Congreso RSME 2013



# S17

## Estadística

**Mar 22, 11:00 - 11:55, Aula 7** – Wenceslao González Manteiga:  
*Goodness-of-fit tests for regression models: the functional data case*

**Mar 22, 12:00 - 12:25, Aula 7** – Juan Carlos Pardo Fernández:  
*On the use of the characteristic function of the residuals to test for the equality of regression curves*

**Mar 22, 12:30 - 12:55, Aula 7** – Carla Moreira:  
*Goodness-of-fit tests for a semiparametric model under random double truncation*

**Mar 22, 13:00 - 13:25, Aula 7** – Pablo Martínez Cambor:  
*A general bootstrap algorithm for hypothesis testing*

**Mar 22, 17:00 - 17:55, Aula 7** – Ricardo Cao:  
*Maximum likelihood estimation for conditional distribution single-index models under censoring*

**Mar 22, 18:00 - 18:25, Aula 7** – María del Carmen Iglesias Pérez:  
*CLT of nonparametric regression estimator with truncated, censored and dependent data*

**Mar 22, 18:30 - 18:55, Aula 7** – Javier Roca Pardiñas:  
*Métodos estadísticos de selección de variables en modelos de regresión multivariantes. Aplicaciones en medioambiente y salud*

**Mar 22, 19:00 - 19:25, Aula 7** – Mar Rodríguez Girondo:  
*Model building in non proportional hazard regression*

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## Goodness-of-fit tests for regression models: the functional data case

Wenceslao González-Manteiga<sup>1</sup>, Juan Cuesta-Albertos<sup>2</sup>, Manuel Febrero-Bande<sup>1</sup>, Eduardo García-Portugués<sup>1</sup>

In this talk the topic of the goodness-of-fit for regression models with functional covariates is considered. Although several papers have been published in the last two decades for the checking of regression models, the case where the covariates are functional is quite recent and has became of interest in the last years. We will review the very recent advances in this area and we will propose a new goodness-of-fit test for the null hypothesis of a functional linear model with scalar response. Our test is based on a generalization to the functional framework of a previous one, designed for the goodness-of-fit of regression models with multivariate covariates using random projections. The test statistic is easy to compute using geometrical and matrix arguments, and simple to calibrate in its distribution by a wild bootstrap on the residuals. Some theoretical aspects are derived and the finite sample properties of the test are illustrated by a simulation study. Finally, the test is applied to real data for checking the assumption of the functional linear model and a graphical tool is introduced.

**Keywords:** Functional Data, Goodness-of-fit, Bootstrap/resampling, Statistical computing

**MSC 2010:** 62G05, 62G09, 62G10

## References

- [1] E. GARCÍA-PORTUGUÉS, W. GONZÁLEZ-MANTEIGA AND M. FEBRERO-BANDE, A goodness-of-fit for the functional linear model. *arXiv:1205.6167* (second revision in *Journal of Computational and Graphical Statistics*).
- [2] L. HORVATH AND P. KOKOSZKA, *Inference for Functional Data With Applications*. Springer, 2012. New York.
- [3] J. O. RAMSAY AND B. W. SILVERMAN, *Functional data analysis*. Springer, 2005. New York.

<sup>1</sup>Department of Statistics and Operations Research  
University of Santiago de Compostela  
Faculty of Mathematics

<sup>2</sup>Department of Mathematics  
University of Cantabria  
Faculty of Sciences

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## On the use of the characteristic function of the residuals to test for the equality of regression curves

Juan Carlos Pardo-Fernández<sup>1</sup>

In this talk we will present a new procedure to test for the equality of  $k$  regression curves in a fully nonparametric context. The test is based on the comparison of two empirical estimators of the characteristic functions of the regression residuals in each population. The asymptotic behaviour of the test statistic is studied in detail. It is shown that, under the null hypothesis, the distribution of the test statistic converges to a combination of independent  $\chi_1^2$  random variables. Under certain restrictions on the populations, the asymptotic null distribution of the test statistic is  $\chi_{k-1}^2$ . The practical performance of the test based on the asymptotic null distribution is investigated by means of simulations.

This is joint work with M. Dolores Jiménez-Gamero (Universidad de Sevilla) and Anouar El Ghouch (Université catholique de Louvain).

**Keywords:** Comparison of regression curves, Empirical characteristic function, Regression residuals.

**MSC 2010:** 62G08, 62G10

<sup>1</sup>Departamento de Estatística e Investigación Operativa  
Universidade de Vigo  
Facultade de Ciencias Económicas e Empresariais  
Campus Universitario As Lagoas-Marcosende  
36310 Vigo (Pontevedra)  
[juancp@uvigo.es](mailto:juancp@uvigo.es)

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## Goodness-of-fit tests for a semiparametric model under random double truncation

Carla Moreira<sup>1,2</sup>, Jacobo de Uña-Álvarez<sup>1</sup>, Ingrid Van Keilegom<sup>3</sup>

Doubly truncated data are commonly encountered in areas like medicine, astronomy, economy, among others. A semiparametric estimator of a doubly truncated random variable has been proposed by [1]. Their estimator is based on a parametric specification of the distribution function of the truncation times. This semiparametric estimator outperforms the nonparametric maximum likelihood estimator when the parametric information is correct, but might behave badly when the assumed parametric model is far off. We introduce several goodness-of-fit tests for the parametric model. The proposed tests are investigated through simulations. For illustration purposes, the tests are also applied to data on the induction time to AIDS for blood transfusion patients.

**Keywords:** Double truncation, goodness-of-fit tests

**MSC 2010:** 62N86, 62G10

## References

- [1] MOREIRA, C. AND DE UÑA-ÁLVAREZ, J., A semiparametric estimator of survival for doubly truncated data. *Statistics in Medicine* **29**, 3147–3159 (2010).

<sup>1</sup>Department of Statistics and OR  
University of Vigo  
Lagoas - Marcosende, 36 310, Vigo - Spain  
carla@uvigo.es, jacobo@uvigo.es

<sup>2</sup>Centro de Matemática da Universidade do Minho  
Campus de Gualtar, 4710 - 057 Braga - Portugal

<sup>3</sup>Institute of Statistics, Biostatistics and Actuarial Sciences  
Université catholique de Louvain  
Voie du Roman Pays 20, B 1348 Louvain-la-Neuve - Belgium  
ingrid.vankeilegom@uclouvain.be

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## A general bootstrap algorithm for hypothesis testing

Pablo Martínez-Camblor<sup>1,2</sup>, Norberto Corral<sup>2</sup>

The bootstrap, introduced and explored in detail by Efron [1] [2], is a intensive computer-based method originally devoted to estimate the standard deviations, confidence intervals and bias of the studied statistic. This technique is useful in a wide variety of statistical procedures, however, its use for hypothesis testing, when the data structure is complex, is not straightforward and each case must be particularly treated. In this work, a general bootstrap algorithm (gBA) for hypothesis testing is studied. The considered method preserves the data structure of each group independently and, in spite of most of the authors match that the resampling under the null is critical to the proper construction of bootstrap test (see, for example, Hall and Wilson [3] or Westfall and Young [4]), in the introduced procedure, the null hypothesis is only used in order to compute the bootstrap statistic values (not at the resampling, as usual). The asymptotic distribution is developed and several case studies are discussed.

**Keywords:** Gini index, Survival model, Competing risk, Cumulative incidence function

**MSC 2010:** 62F03, 62F40

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- [4] P.H. WESTFALL, S.S. YOUNG, (1993) *Resampling-based Multiple Testing: Examples and Methods for p-value Adjustment*, Wiley, New York.

<sup>1</sup>Oficina de Investigación Biosanitaria de Asturias  
pablomc@ficyt.es

<sup>2</sup>Departamento de Estadística e IO y DM  
Universidad de Oviedo  
[norbert@uniovi.es](mailto:norbert@uniovi.es)

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## Maximum likelihood estimation for conditional distribution single-index models under censoring<sup>\*</sup>

Ricardo Cao<sup>1</sup>, Ewa Strzalkowska-Kominiak<sup>2</sup>

A new likelihood approach is proposed for the problem of semiparametric estimation of a conditional distribution or density under censoring. Consistency and asymptotic normality for two versions of the maximum likelihood estimator of the parameter vector in the single index model are proved. The single-index model considered can be seen as a useful tool for credit scoring and estimation of the default probability in credit risk. A data-driven bandwidth selection procedure is proposed. It allows to choose the smoothing parameter involved in our approach. The finite sample performance of the estimators has been studied by simulations, where the new method has been compared with the method proposed by Bouaziz and Lopez (2010) [1]. To the best of our knowledge this is the only existing competitor in this context. The simulation study shows the good behavior of the proposed method.

**Keywords:** conditional density function, credit risk, kernel estimation, survival analysis

**MSC 2010:** 62G07, 62G20, 62N01, 62N02

## References

- [1] O. BOUAZIZ, O. LOPEZ, Conditional density estimation in a censored single-index model. *Bernoulli* **16**, 514–542 (2010).

<sup>1</sup>Departamento de Matemáticas  
Universidade da Coruña  
Facultade de Informática, Campus de Elviña, 15071 A Coruña, Spain  
rcao@udc.es

<sup>2</sup>Departamento de Estadística  
Universidad Carlos III de Madrid  
C/ Madrid, 126, 28903 Getafe (Madrid) Spain  
ewa.strzalkowska@uc3m.es

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\*MINECO Grants MTM2008-00166 and MTM2011-22392 (EU ERDF support included)

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## **CLT of nonparametric regression estimator with truncated, censored and dependent data**

**Liang, Han-Ying<sup>1</sup>; de Uña-Álvarez, Jacobo<sup>2</sup>; Iglesias-Pérez, María del  
Carmen<sup>3</sup>**

We propose a method to estimate the regression function under a left truncation and right censored model. It is assumed that the observations form a stationary  $\alpha$ -mixing sequence. The new estimators are based on the idea of the Nadaraya-Watson and the local lineal smoothers applied to a certain transformation of the data. Asymptotic normality of the estimators is established. Their finite sample behavior is also investigated in a simulation study.

**Keywords:** Asymptotic normality, Nadaraya-Watson and local linear smoothing, regression function, truncated and censored data,  $\alpha$ -mixing.

**MSC 2010:** 62N01, 62E20.

<sup>1</sup>Department of Mathematics  
Tongji University  
Shanghai 200092. P.R. China  
hyliang83@yahoo.com

<sup>2</sup>Departamento de Estadística e Investigación Operativa  
Universidad de Vigo  
Facultad de Ciencias Económicas y Empresariales.  
Campus Lagoas-Marcosende. 36310 Vigo. España  
jacobo@uvigo.es

<sup>3</sup>Departamento de Estadística e Investigación Operativa  
Universidad de Vigo  
Escuela de Ingeniería Forestal.  
Campus A Xunqueira. 36005 Pontevedra. España  
mcigles@uvigo.es

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## **Métodos estadísticos de selección de variables en modelos de regresión multivariantes. Aplicaciones en salud**

**Javier Roca Pardiñas<sup>1</sup>**

En muchas aplicaciones biomédicas, el interés reside en ser capaz de distinguir entre dos posibles estados de una variable de respuesta dada, dependiendo de los valores de determinados predictores. Si el número de predictores es elevado, o si existe una redundancia entre ellos, entonces será muy importante decidir sobre el mejor subconjunto de predictores que dará lugar el modelo con mejor capacidad de discriminación. Con este objetivo, se han considerado los modelos aditivos generalizados de respuesta binaria, y se ha utilizado la “receiver operating characteristic (ROC) ” con el fin de determinar y comparar la capacidad discriminatoria de tales modelos. En este estudio se han desarrollado pruebas basadas en el remuestreo bootstrap que permiten: a) obtener el número óptimo de predictores; y b) el modelo o modelos con ese número de predictores, que presentan el mayor AUC (área bajo la curva ROC). El método propuesto se aplicó a un sistema de diagnóstico asistido por ordenador dedicado a la detección precoz del cáncer de mama.

<sup>1</sup>Departamento de Estatística e I.O  
Universidade de Vigo  
E.U. Ingeniería Industrial  
C/Torrecedeira 86, 36208  
Vigo (Pontevedra)  
roca@uvigo.es

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## Model building in non proportional hazard regression

**Mar Rodríguez-Girondo<sup>1</sup>, Thomas Kneib<sup>2</sup>, Carmen Cadarso-Suárez<sup>3</sup>, Emad Abu-Assi<sup>4</sup>**

Recent developments of statistical methods allow for a very flexible modeling of covariates affecting survival times via the hazard rate, including also the inspection of possible timedeependent associations. Despite their immediate appeal in terms of flexibility, these models typically introduce additional difficulties when a subset of covariates and the corresponding modeling alternatives have to be chosen, i.e. for building the most suitable model for given data. This is particularly true when potentially time-varying associations are given. We propose to conduct a piecewise exponential representation of the original survival data to link hazard regression with estimation schemes based on the Poisson likelihood to make recent advances for model building in exponential family regression accessible also in the non proportional hazard regression context. A two-stage stepwise selection approach, an approach based on doubly penalized likelihood and a componentwise functional gradient descent approach will be adapted to the piecewise exponential regression problem and compared via an intensive simulation study. An application to prognosis after discharge for patients who suffered a myocardial infarction supplements the simulation to demonstrate the pros and cons of the approaches in real data analyses.

**Keywords:** Survival analysis, Variable selection, Model Choice, Boosting, Generalized additive models

**MSC 2010:** 62P10, 62N01,6207

<sup>1</sup>siDOR Research Group  
University of Vigo  
Facultade de Ciencias Económicas e Empresariais  
Campus Lagoas-Marcosende  
Vigo, SPAIN  
[margirondo@uvigo.es](mailto:margirondo@uvigo.es)

<sup>2</sup>Center for Statistics and Econometrics  
Georg August University  
Platz der Göttinger Sieben 5  
Göttingen, GERMANY  
[tkneib@uni-goettingen.de](mailto:tkneib@uni-goettingen.de)

<sup>3</sup>Unit of Biostatistics, Department of Statistics  
University of Santiago de Compostela  
Facultade de Medicina e Odontoloxía  
Rúa San Francisco s/n  
Santiago de Compostela, SPAIN  
[carmen.cadarso@usc.es](mailto:carmen.cadarso@usc.es)

<sup>4</sup>Department of Cardiology  
Hospital Clínico de Santiago de Compostela  
Facultade de Medicina e Odontoloxía  
A Choupana s/n  
Santiago de Compostela, SPAIN  
[eabuassi@yahoo.es](mailto:eabuassi@yahoo.es)